CLAIMS

1   1. A fine-to-coarse level mesh generating arrangement for generating a coarse level mesh
2   representation representing a surface, from a finer level mesh representation comprising:

3   A.   an indicator value generator module configured to, for respective ones of the points in the
4   finer level surface representation, evaluate an indicator function to generate an indicator
5   value, the indicator value indicating whether one a subdivision-inverse filter methodology
6   or a least-squares optimization methodology is to be used to determine a position for a
7   corresponding point in the coarse level mesh representation; and

8   B.   a coarse level mesh generator module configured to determine, for each of the points that are
9   to be provided in the coarse level mesh representation, a position in the coarse level mesh
10   representation in response to the position of the corresponding point in the finer level mesh
11   representation, in accordance with the one of the subdivision-inverse filter methodology and
12   least-squares optimization methodology as indicated by the indicator value generated by the
13   indicator value generator module.

1   2. An arrangement as defined in claim 1 further comprising a Laplacian generator module configured
2   to generate a Laplacian value for said respective ones of the points in the finer level mesh
3   representation.

1   3. An arrangement as defined in claim 2 in which the Laplacian generator module is configured to
2   generate the Laplacian value L(k,j+1), for at least one of said points, said at least one of said points
3   comprising a point on a boundary, crease line or the like in a triangular mesh representation, in
4   accordance with

$$L(k, j+1) \ = \ \frac{1}{2}\left[c^{J+1}(k-1) + c^{J+1}(k+1)\right] - c^{J+1}(k)$$

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5   where $c^{j+1}(k)$ represents the position of the point for which the Laplacian is being generated in the

6   finer level mesh representation, and $c^{j+1}(k-1)$ and $c^{j+1}(k+1)$ represent the positions of neighboring

7   points in the finer level mesh representation.

1   4. An arrangement as defined in claim 2 in which the Laplacian generator module is configured to

2   generate the Laplacian value L(k,j+1), for at least one of said points, said at least one of said points

3   comprising a regular vertex, that is, for a vertex for which the valence "K" is equal to "six," in a

4   triangular mesh representation, in accordance with

$$L(k,j+1) \;=\; \frac{1}{6}\left(\sum_{l \in N(k,j+1)} c^{J+1}(l) \right) - c^{J+1}(k)$$

5   where $c^{j+1}(k)$ represents the position of the point for which the Laplacian is being generated in the

6   finer level mesh representation, and $c^{j+1}(l)$ represents the positions of neighboring points in the finer

7   level mesh representation.

1   5. An arrangement as defined in claim 2 in which the Laplacian generator module is configured to

2   generate the Laplacian value L(k,j+1), for at least one of said points, said at least one of said points

3   comprising a for a irregular vertex, that is, for a vertex for which the valence "K" is not equal to

4   "six," in a triangular mesh representation, in accordance with

$$L(k,j+1) \;=\; \rho \left[\frac{1}{K} \sum_{l \in N(k,j+1)} c^{J+1}(l) - c^{J+1}(k) \right]$$

5   where $c^{j+1}(k)$ represents the position of the point for which the Laplacian is being generated in the

6   finer level mesh representation, and $c^{j+1}(l)$ represents the positions of neighboring points in the finer

7   l e v e l   m e s h   r e p r e s e n t a t i o n , $\rho = -\dfrac{3 + 8\,a(K)}{3\left(-5 + 8\,a(K)\right)}$,   a n d

8

$$a(K) = \frac{5}{8} - \left(\frac{3 + 2\cos\left(\dfrac{2\pi}{K}\right)}{8}\right)^2 .$$

1   6. An arrangement as defined in claim 2 in which the Laplacian generator module is configured to

2   generate the Laplacian value L(k,j+1), for at least one of said points, said at least one of said points

3   comprising a point on a boundary, crease line or the like in a quadrilateral mesh representation, in

4   accordance with

$$L(k, j+1) = \frac{1}{2}\left(c^{j+1}(k-1) + c^{j+1}(k+1)\right) - c^{j+1}(k) \tag{47}$$

5   where $c^{j+1}(k)$ is the position of the vertex for which the Laplacian is being generated, and $c^{j+1}(k-1)$

6   and $c^{j+1}(k+1)$ are the positions of the neighboring points in the fine level mesh representation.

1   7. An arrangement as defined in claim 2 in which the Laplacian generator module is configured to

2   generate Laplacian values $L_e(k,j+1)$ and $L_f(k,j+1)$, for at least one of said points, said at least one of

3   said points comprising a point on a boundary, crease line or the like in a quadrilateral mesh

4   representation, in accordance with

$$L_e(k, j+1) \;=\; \frac{1}{K}\left(\sum_{l \in N_e(k,J+1)} c^{J+1}(l) \right) - c^{J+1}(k)$$

and

$$L_f(k, j+1) \;=\; \frac{1}{K}\left(\sum_{l \in N_f(k,J+1)} c^{J+1}(l) \right) - c^{J+1}(k)$$

6   where $N_e(k,j+1)$ references a set of points comprising first order neighbors of the at least one of said

7   points in the finer level mesh representation, and $N_f(k,j+1)$ references a set of points comprising

8   second order neighbors of the at least one operating system said points in the finer level mesh

9   representation.

1   8. An arrangement as defined in claim 7 in which the coarse level mesh generator module is

2   configured to determine, for at least one of the points that are to be provided in the coarse level mesh

3   representation, the position in the coarse level mesh representation as the position of the

4   corresponding point in the finer level mesh representation if the magnitude both Laplacian values

5    $L_e(k,j+1)$ and $L_f(k,j+1)$ generated by the Laplacian generator module are below a predetermined

6   threshold value.

1   9. An arrangement as defined in claim 2 in which the coarse level mesh generator module is

2   configured to determine, for at least one of the points that are to be provided in the coarse level mesh

3   representation, the position in the coarse level mesh representation as the position of the

4   corresponding point in the finer level mesh representation if the magnitude of the Laplacian value

5   generated by the Laplacian generator module is below a predetermined threshold value.

10. An arrangement as defined in claim 2 in which the coarse level mesh generator module is

configured to determine, for each of the points that are to be provided in the coarse level mesh

representation, a position in the coarse level mesh representation in response to the position of the

corresponding point in the finer level mesh representation, in accordance with the subdivision-

inverse filter methodology if the magnitude of the indicator value is below a selected threshold

value.

1   11. An arrangement as defined in claim 10 in which the coarse level mesh generator module is

2   configured to determine, for at least one of said points, comprising a point on a boundary, crease line

3   or the like in a triangular mesh representation, for which the magnitude of the indicator value is

4   below the selected threshold value, a position $c^j(k)$ in the coarse level mesh representation in

5   accordance with

$$c^j(k) \;=\; c^{j+1}(k) + \lambda\, L(k, j+1)$$

6   where $c^{j+1}(k)$ represents the position of the corresponding point in the finer level mesh representation,

7     $L(k,j+1)$ represents the Laplacian value generated by the Laplacian generator module for the point

8   in the finer level mesh representation, and λ represents a parameter whose value is $\lambda = -1$.

1   12. An arrangement as defined in claim 10 in which the coarse level mesh generator module is

2   configured to determine, for at least one of said points in a triangular mesh representation,

3   comprising a regular point, that is, a point whose valence "K" is equal to "six," and is not on a

4   boundary, crease line or the like, for which the magnitude of the indicator value is below the selected

5   threshold value, a position $c^j(k)$ in the coarse level mesh representation in accordance with

$$c^j(k) = c^{j+1}(k) + \lambda\, L(k,j+1)$$

6   where $c^{j+1}(k)$ represents the position of the corresponding point in the finer level mesh representation,

7     $L(k,j+1)$ represents the Laplacian value generated by the Laplacian generator module for the point

8   in the finer level mesh representation, and λ represents a parameter whose value is $\lambda = -\dfrac{3}{2}$.

1   13. An arrangement as defined in claim 10 in which the coarse level mesh generator module is

2   configured to determine, for at least one of said points in a triangular mesh representation,

3   comprising an irregular point, that is, a point whose valence "K" is not equal to "six," and is not on

4   a boundary, crease line or the like, for which the magnitude of the indicator value is below the

5   selected threshold value, a position $c^j(k)$ in the coarse level mesh representation in accordance with

$$c^J(k) = c^{J+1}(k) + \lambda\, L(k, j+1)$$

6   where $c^{j+1}(k)$ represents the position of the corresponding point in the finer level mesh representation,

7   L(k,j+1) represents the Laplacian value generated by the Laplacian generator module for the point

8   in the finer level mesh representation, and λ represents a parameter whose value is generated in

9   accordance with $\quad \lambda = \dfrac{8\,a(K)}{-5 + 8\,a(K)}$, where $a(K) = \dfrac{5}{8} - \left(\dfrac{3 + 2\cos\left(\dfrac{2\pi}{K}\right)}{8}\right)^2$.

1   14. An arrangement as defined in claim 10 in which the coarse level mesh generator module is

2   configured to determine, for at least one of said points, comprising a point on a boundary, crease line

3   or the like in a quadrilateral mesh representation, for which the magnitude of the indicator value is

4   below the selected threshold value, a position $c^j(k)$ in the coarse level mesh representation in

5   accordance with

$$c^J(k) = c^{J+1}(k) + \lambda\, L(k, j+1)$$

6 where $c^{j+1}(k)$ represents the position of the corresponding point in the finer level mesh representation,

7 $L(k,j+1)$ represents the Laplacian value generated by the Laplacian generator module for the point

8 in the finer level mesh representation, and λ represents a parameter whose value is $\lambda = -1$.

1 15. An arrangement as defined in claim 10 in which the coarse level mesh generator module is

2 configured to determine, for at least one of said points in a quadrilateral mesh representation, which

3 is not on a boundary, crease line or the like, for which the magnitude of the indicator value is below

4 the selected threshold value, a position $c^j(k)$ in the coarse level mesh representation in accordance

5 with

$$c^J(k) = c^{J+1}(k) + \lambda_1 L_e(k, j+1) + \lambda_2 L_f(k, j+1)$$

6 where $c^{j+1}(k)$ represents the position of the corresponding point in the finer level mesh representation,

7 $L_e(k,j+1)$ and $L_f(k,j+1)$ represent Laplacian values generated by the Laplacian generator module for

8 the point in the finer level mesh representation, and λ_1 and λ_2 represent parameters whose values are

9 generated in accordance with, if the valence "K" of the point not equal to "three,"

$$\lambda_1 = -\frac{4}{K-3}$$

$$\lambda_2 = \frac{1}{K-3}$$

10 and, if the valence "K" for the vertex is equal to "three,"

$$\lambda_1 = -8, \quad \lambda_2 = 2$$

.

1 16. An arrangement as defined in claim 2 in which the coarse level mesh generator module is

2 configured to determine, for each of the points that are to be provided in the coarse level mesh

3 representation, a position in the coarse level mesh representation in response to the position of the

4 corresponding point in the finer level mesh representation, in accordance with the least-squares

5 optimization methodology if the magnitude of the indicator value is above a selected threshold value.

1 17. An arrangement as defined in claim 16 in which the coarse level mesh generator module is

2 configured to determine, for at least one of said points, comprising a point on a boundary, crease line

3 or the like in a triangular mesh representation, for which the magnitude of the indicator value is not

4 below the selected threshold value, a position $c^j(k)$ in the coarse level mesh representation in

5 accordance with

$$c^J(k) = c^{J+1}(k) + \lambda \, L(k, j+1)$$

6 where $c^{j+1}(k)$ represents the position of the corresponding point in the finer level mesh representation,

7 L(k,j+1) represents the Laplacian value generated by the Laplacian generator module for the point

8 in the finer level mesh representation, and λ represents a parameter whose value is generated in

9 accordance with

$$\lambda = \frac{1}{L(k)} \left[b_0^{1D} \, L(k) + \frac{1}{2} b_1^{1D} \left(L(k-1) + L(k+1) \right) \right]$$

10 where $b_0^{1D} = -\dfrac{12}{35}$ and $b_1^{1D} = -\dfrac{23}{49}$, and L(k-1) and L(k+1) represent Laplacian values generated

11 by the Laplacian generator module for neighboring points in the finer level mesh representation.

18. An arrangement as defined in claim 16 in which the coarse level mesh generator module is configured to determine, for at least one of said points in a triangular mesh representation, comprising a regular point, that is, a point whose valence "K" is equal to "six," and is not on a boundary, crease line or the like, for which the magnitude of the indicator value is not below the selected threshold value, a position $c^j(k)$ in the coarse level mesh representation in accordance with

$$c^J(k) = c^{J+1}(k) + \lambda \, L(k, j+1)$$

6 where $c^{j+1}(k)$ represents the position of the corresponding point in the finer level mesh representation,

7 L(k,j+1) represents the Laplacian value generated by the Laplacian generator module for the point

8 in the finer level mesh representation, and λ represents a parameter whose value is

$$\lambda = \frac{1}{L(k)} \left[b_0^{reg} \, L(k) + \frac{1}{6} b_1^{reg} \sum_{l \in N(k,j+1)} L(l) \right]$$

9   where $b_0^{reg} = -\dfrac{61}{5720}$ and $b_1^{reg} = -\dfrac{14403}{5720}$ and L(l) represent Laplacian values generated by the

10   Laplacian operator for points, identified by indices N(k,j+1), that neighbor the at least one of said

11   points.

1   19. An arrangement as defined in claim 16 in which the coarse level mesh generator module is

2   configured to determine, for at least one of said points in a triangular mesh representation,

3   comprising an irregular point, that is, a point whose valence "K" is not equal to "six," and is not on

4   a boundary, crease line or the like, for which the magnitude of the indicator value is below the

5   selected threshold value, a position $c^j(k)$ in the coarse level mesh representation in accordance with

$$c^j(k) \;=\; c^{j+1}(k) + \lambda \, L(k, j+1)$$

6   where $c^{j+1}(k)$ represents the position of the corresponding point in the finer level mesh representation,

7   L(k,j+1) represents the Laplacian value generated by the Laplacian generator module for the point

8   in the finer level mesh representation, and λ represents a parameter whose value is generated in

9   accordance with $\lambda \;=\; \dfrac{1}{L(k)}\left[b_0^{irreg} \, L(k) + \dfrac{1}{K} b_1^{irreg} \sum_{l \in N(k,j+1)} L(l) \right]$, where

$$b_0^{irreg} \;=\; \frac{2\left(5 - 8a(K)\right)\left(14647\,K - 391848\,a(K) + 391848\,a(k)^2\right)}{715\left(3 + 8\,a(k)\right)\left(256 + 41K - 512\,a(k) + 256\,a(k)^2\right)}$$

10   and

$$b_1^{irreg} = \frac{16\left(-5531K - 24521\,a(K) + 24521\,a(K)^2\right)}{715\left(256 + 41K - 512\,a(K) + 25\,a(K)^2\right)}$$

11   and where $a(K) = \dfrac{5}{8} - \left(\dfrac{3 + 2\cos\left(\dfrac{2\pi}{K}\right)}{8}\right)^2 .$

1   20. An arrangement as defined in claim 16 in which the coarse level mesh generator module is
2   configured to determine, for at least one of said points, comprising a point on a boundary, crease line
3   or the like in a quadrilateral mesh representation, for which the magnitude of the indicator value is
4   not below the selected threshold value, a position $c^j(k)$ in the coarse level mesh representation in
5   accordance with

$$c^J(k) = c^{J+1}(k) + \lambda\, L(k, j+1)$$

6   where $c^{j+1}(k)$ represents the position of the corresponding point in the finer level mesh representation,

7    $L(k,j+1)$ represents the Laplacian value generated by the Laplacian generator module for the point

8   in the finer level mesh representation, and λ represents a parameter whose value is generated in

9   accordance with

$$\lambda = \frac{1}{L(k)}\left[b_0^{1D}\, L(k) + \frac{1}{2} b_1^{1D} \left(L(k-1) + L(k+1) \right) \right]$$

10   where $b_0^{1D} = -\dfrac{12}{35}$ and $b_1^{1D} = -\dfrac{23}{49}$, and L(k-1) and L(k+1) represent Laplacian values generated

11   by the Laplacian generator module for neighboring points in the finer level mesh representation.

21. An arrangement as defined in claim 16 in which the coarse level mesh generator module is

configured to determine, for at least one of said points in a quadrilateral mesh representation, which

is not on a boundary, crease line or the like, for which the magnitude of the indicator value is below

the selected threshold value, a position $c^j(k)$ in the coarse level mesh representation in accordance

with

$$c^J(k) = c^{J+1}(k) + \lambda_1\, L_e\!\left(k, j+1\right) + \lambda_2\, L_f\!\left(k, j+1\right)$$

6   where $c^{j+1}(k)$ represents the position of the corresponding point in the finer level mesh representation,

7    $L_e(k,j+1)$ and $L_f(k,j+1)$ represent Laplacian values generated by the Laplacian generator module for

8   the point in the finer level mesh representation, and λ_1 and λ_2 represent parameters whose values are

9   generated in accordance with

$$\lambda_1 = \frac{1}{L_e(k,j+1)}\left[b_{10}^{cc}\,L_c(k,j+1)+\frac{1}{K}b_{11}^{cc}\sum_{l\in N(k,j+1)}L_e(l,j+1)\right]$$

10   and

$$\lambda_2 = \frac{1}{L_f(k,j+1)}\left[b_{20}^{cc}\,L_f(k,j+1)+\frac{1}{K}b_{21}^{cc}\sum_{l\in N_f(k,j+1)}L_f(l,j+1)\right]$$

where, if the at least one of said points is regular, that is, if its valence "K" is "four,"

$$b_{10}^{cc} = -\frac{9946871}{4862025}$$

$$b_{11}^{cc} = -\frac{1024}{405}$$

$$b_{20}^{cc} = \frac{1644032}{972405}$$

$$b_{21}^{cc} = -\frac{1338874}{972405}$$

12   and, if the at least one point is irregular, that is, its valence "K" is other than "four,"

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$$b_{10}^{cc} = \frac{162307143936 - 92746939392\,K - 8924282387\,K^3}{4862025\left(12544 - 14336\,K + 4096\,K^2 + 901\,K^3\right)}$$

$$b_{11}^{cc} = \frac{1024\left(2793728 - 1596416\,K - 244001\,K^3\right)}{99225\left(12544 - 14336\,K + 4096\,K^2 + 901\,K^3\right)}$$

$$b_{20}^{cc} = \frac{512\left(-113305472 + 64745984\,K + 17391149\,K^3\right)}{4862025\left(12544 - 14336\,K + 4096\,K^2 + 901\,K^3\right)}$$

$$b_{21}^{cc} = \frac{4\left(8660934688 - 4949105536\,K - 1876158821\,K^3\right)}{4862025\left(12544 - 14336\,K + 4096\,K^2 + 901\,K^3\right)}$$

22. A method of generating a coarse level mesh representation representing a surface, from a finer level mesh representation including the steps of:

A.   indicator value generator step of, for respective ones of the points in the finer level mesh representation, evaluating an indicator function to generate an indicator value, the indicator value indicating whether one a subdivision-inverse filter methodology or a least-squares optimization methodology is to be used to determine a position for a corresponding point in the coarse level mesh representation; and

B.   a coarse level mesh generator step of determining, for each of the points that are to be provided in the coarse level mesh representation, a position in the coarse level mesh representation in response to the position of the corresponding point in the finer level mesh representation, in accordance with the one of the subdivision-inverse filter methodology and least-squares optimization methodology as indicated by the indicator value generated during the indicator value generator step.

1   23. A method as defined in claim 22 further comprising a Laplacian generator step of generating a

2   Laplacian value for said respective ones of the points in the finer level mesh representation.

1   24. A method as defined in claim 23 in which the Laplacian generator step includes the step of

2   generating the Laplacian value L(k,j+1), for at least one of said points, said at least one of said points

3   comprising a point on a boundary, crease line or the like in a triangular mesh representation, in

4   accordance with

$$L(k, j+1) = \frac{1}{2}\left[c^{j+1}(k-1) + c^{j+1}(k+1)\right] - c^{j+1}(k)$$

where $c^{j+1}(k)$ represents the position of the point for which the Laplacian is being generated in the finer level mesh representation, and $c^{j+1}(k-1)$ and $c^{j+1}(k+1)$ represent the positions of neighboring points in the finer level mesh representation.

1   25. A method as defined in claim 23 in which the Laplacian generator step includes the step of

2   generating the Laplacian value L(k,j+1), for at least one of said points, said at least one of said points

3   comprising a regular vertex, that is, for a vertex for which the valence "K" is equal to "six," in a

4   triangular mesh representation, in accordance with

$$L(k, j+1) = \frac{1}{6}\left(\sum_{l \in N(k, j+1)} c^{j+1}(l)\right) - c^{j+1}(k)$$

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5   where $c^{j+1}(k)$ represents the position of the point for which the Laplacian is being generated in the

6   finer level mesh representation, and $c^{j+1}(l)$ represents the positions of neighboring points in the finer

7   level mesh representation.

1   26. A method as defined in claim 23 in which the Laplacian generator step includes the step of

2   generating the Laplacian value L(k,j+1), for at least one of said points, said at least one of said points

3   comprising a for a irregular vertex, that is, for a vertex for which the valence "K" is not equal to

4   "six," in a triangular mesh representation, in accordance with

$$L(k,j+1) \; = \; \rho\left[\frac{1}{K}\sum_{l\in N(k,j+1)}c^{j+1}(l) - c^{j+1}(k)\right]$$

5   where $c^{j+1}(k)$ represents the position of the point for which the Laplacian is being generated in the

6   finer level mesh representation, and $c^{j+1}(l)$ represents the positions of neighboring points in the finer

7   l e v e l   m e s h   r e p r e s e n t a t i o n , $\rho \; = \; -\dfrac{3+8\,a(K)}{3\left(-5+8\,a(K)\right)},$ a n d

8    $$a(K) \; = \; \frac{5}{8} - \left(\frac{3+2\cos\left(\dfrac{2\pi}{K}\right)}{8}\right)^{2}.$$

1   27. A method as defined in claim 23 in which the Laplacian generator step includes the step of

2   generating the Laplacian value L(k,j+1), for at least one of said points, said at least one of said points

3   comprising a point on a boundary, crease line or the like in a quadrilateral mesh representation, in

4   accordance with

$$L(k, j+1) \;=\; \frac{1}{2}\left(c^{J+1}(k-1) + c^{J+1}(k+1)\right) - c^{J+1}(k) \qquad (74)$$

where $c^{J+1}(k)$ is the position of the vertex for which the Laplacian is being generated, and $c^{j+1}(k-1)$ and $c^{j+1}(k+1)$ are the positions of the neighboring points in the fine level mesh representation.

28. A method as defined in claim 23 in which the Laplacian generator step includes the step of generating Laplacian values $L_e(k,j+1)$ and $L_f(k,j+1)$, for at least one of said points, said at least one of said points comprising a point on a boundary, crease line or the like in a quadrilateral mesh representation, in accordance with

$$L_e(k, j+1) \;=\; \frac{1}{K}\left(\sum_{l \in N_e(k,j+1)} c^{J+1}(l)\right) - c^{J+1}(k)$$

5   and

$$L_f(k, j+1) \;=\; \frac{1}{K}\left(\sum_{l \in N_f(k,J+1)} c^{J+1}(l)\right) - c^{J+1}(k)$$

6   where $N_e(k,j+1)$ references a set of points comprising first order neighbors of the at least one of said

7   points in the finer level mesh representation, and $N_f(k,j+1)$ references a set of points comprising

8   second order neighbors of the at least one operating system said points in the finer level mesh

9   representation.

1   29. A method as defined in claim 28 in which the coarse level mesh generator step includes the step

2   of determining, for at least one of the points that are to be provided in the coarse level mesh

3   representation, the position in the coarse level mesh representation as the position of the

4   corresponding point in the finer level mesh representation if the magnitude both Laplacian values

5     $L_e(k,j+1)$ and $L_f(k,j+1)$ generated during the Laplacian generator step are below a predetermined

6   threshold value.

1   30. A method as defined in claim 23 in which the coarse level mesh generator step includes the step

2   of determining, for at least one of the points that are to be provided in the coarse level mesh

3   representation, the position in the coarse level mesh representation as the position of the

4   corresponding point in the finer level mesh representation if the magnitude of the Laplacian value

5   generated during the Laplacian generator step is below a predetermined threshold value.

1   31. A method as defined in claim 23 in which the coarse level mesh generator step includes the step

2   of determining, for each of the points that are to be provided in the coarse level mesh representation,

3   a position in the coarse level mesh representation in response to the position of the corresponding

4   point in the finer level mesh representation, in accordance with the subdivision-inverse filter

5   methodology if the magnitude of the indicator value is below a selected threshold value.

1   32. A method as defined in claim 31 in which the coarse level mesh generator step includes the step

2   of determining, for at least one of said points, comprising a point on a boundary, crease line or the

3 like in a triangular mesh representation, for which the magnitude of the indicator value is below the

4 selected threshold value, a position $c^j(k)$ in the coarse level mesh representation in accordance with

$$c^J(k) \quad = \quad c^{J+1}(k) + \lambda\ L(k, j+1)$$

5 where $c^{j+1}(k)$ represents the position of the corresponding point in the finer level mesh representation,

6 $L(k,j+1)$ represents the Laplacian value generated during the Laplacian generator step for the point

7 in the finer level mesh representation, and λ represents a parameter whose value is $\lambda = -1$.

33. A method as defined in claim 32 in which the coarse level mesh generator step includes the step

of determining, for at least one of said points in a triangular mesh representation, comprising a

regular point, that is, a point whose valence "K" is equal to "six," and is not on a boundary, crease

line or the like, for which the magnitude of the indicator value is below the selected threshold value,

a position $c^j(k)$ in the coarse level mesh representation in accordance with

$$c^J(k) \quad = \quad c^{J+1}(k) + \lambda\ L(k, j+1)$$

6 where $c^{j+1}(k)$ represents the position of the corresponding point in the finer level mesh representation,

7 $L(k,j+1)$ represents the Laplacian value generated during the Laplacian generator step for the point

8 in the finer level mesh representation, and λ represents a parameter whose value is $\lambda = -\dfrac{3}{2}$.

1   34. A method as defined in claim 31 in which the coarse level mesh generator step includes the step

2   of determining, for at least one of said points in a triangular mesh representation, comprising an

3   irregular point, that is, a point whose valence "K" is not equal to "six," and is not on a boundary,

4   crease line or the like, for which the magnitude of the indicator value is below the selected threshold

5   value, a position $c^j(k)$ in the coarse level mesh representation in accordance with

$$c^j(k) \;=\; c^{j+1}(k) + \lambda\, L(k, j+1)$$

where $c^{j+1}(k)$ represents the position of the corresponding point in the finer level mesh representation, $L(k,j+1)$ represents the Laplacian value generated during the Laplacian generator step for the point in the finer level mesh representation, and λ represents a parameter whose value is generated in

accordance with $\lambda \;=\; \dfrac{8\,a(K)}{-5 + 8\,a(K)}$, where $a(K) \;=\; \dfrac{5}{8} - \left(\dfrac{3 + 2\cos\left(\dfrac{2\pi}{K}\right)}{8} \right)^2$.

1   25. A method as defined in claim 31 in which the coarse level mesh generator step includes the step

2   of determining, for at least one of said points, comprising a point on a boundary, crease line or the

3   like in a quadrilateral mesh representation, for which the magnitude of the indicator value is below

4   the selected threshold value, a position $c^j(k)$ in the coarse level mesh representation in accordance

5   with

$$c^J(k) \;\; = \;\; c^{J+1}(k) + \lambda \; L\big(k, j+1\big)$$

6   where $c^{j+1}(k)$ represents the position of the corresponding point in the finer level mesh representation,

7     $L(k,j+1)$ represents the Laplacian value generated during the Laplacian generator step for the point

8   in the finer level mesh representation, and λ represents a parameter whose value is $\lambda \;\; = \;\; -1$.

1   36. A method as defined in claim 31 in which the coarse level mesh generator step includes the step

2   of determining, for at least one of said points in a quadrilateral mesh representation, which is not on

3   a boundary, crease line or the like, for which the magnitude of the indicator value is below the

4   selected threshold value, a position $c^j(k)$ in the coarse level mesh representation in accordance with

$$c^J(k) \;\; = \;\; c^{J+1}(k) + \lambda_1 \, L_e\big(k, j+1\big) + \lambda_2 \, L_f\big(k, j+1\big)$$

5   where $c^{j+1}(k)$ represents the position of the corresponding point in the finer level mesh representation,

6     $L_e(k,j+1)$ and $L_f(k,j+1)$ represent Laplacian values generated during the Laplacian generator step for

7   the point in the finer level mesh representation, and λ_1 and λ_2 represent parameters whose values are

8   generated in accordance with, if the valence "K" of the point not equal to "three,"

$$\lambda_1 = -\frac{4}{K-3}$$

$$\lambda_2 = \frac{1}{K-3}$$

9   and, if the valence "K" for the vertex is equal to "three,"

$$\lambda_1 = -8, \quad \lambda_2 = 2$$

1   37. A method as defined in claim 23 in which the coarse level mesh generator step includes the step of determining, for each of the points that are to be provided in the coarse level mesh representation, a position in the coarse level mesh representation in response to the position of the corresponding point in the finer level mesh representation, in accordance with the least-squares optimization methodology if the magnitude of the indicator value is above a selected threshold value.

1   38. A method as defined in claim 37 in which the coarse level mesh generator step includes the step
2   of determining, for at least one of said points, comprising a point on a boundary, crease line or the
3   like in a triangular mesh representation, for which the magnitude of the indicator value is not below
4   the selected threshold value, a position $c^j(k)$ in the coarse level mesh representation in accordance
5   with

$$c^j(k) = c^{j+1}(k) + \lambda\, L(k, j+1)$$

6 where $c^{j+1}(k)$ represents the position of the corresponding point in the finer level mesh representation,

7 $L(k,j+1)$ represents the Laplacian value generated during the Laplacian generator step for the point

8 in the finer level mesh representation, and λ represents a parameter whose value is generated in

9 accordance with

$$\lambda \;=\; \frac{1}{L(k)}\left[b_0^{1D}\, L(k) + \frac{1}{2} b_1^{1D}\left(L(k-1) + L(k+1)\right)\right]$$

10 where $b_0^{1D} = -\dfrac{12}{35}$ and $b_1^{1D} = -\dfrac{23}{49}$, and L(k-1) and L(k+1) represent Laplacian values generated

11 during the Laplacian generator step for neighboring points in the finer level mesh representation.

1 39. A method as defined in claim 37 in which the coarse level mesh generator step includes the step

2 of determining, for at least one of said points in a triangular mesh representation, comprising a

3 regular point, that is, a point whose valence "K" is equal to "six," and is not on a boundary, crease

4 line or the like, for which the magnitude of the indicator value is not below the selected threshold

5 value, a position $c^j(k)$ in the coarse level mesh representation in accordance with

$$c^j(k) \;=\; c^{j+1}(k) + \lambda\, L\left(k, j+1\right)$$

6 where $c^{j+1}(k)$ represents the position of the corresponding point in the finer level mesh representation,

7 $L(k,j+1)$ represents the Laplacian value generated during the Laplacian generator step for the point

8 in the finer level mesh representation, and λ represents a parameter whose value is

$$\lambda = \frac{1}{L(k)}\left[b_0^{reg}\ L(k) + \frac{1}{6}b_1^{reg}\sum_{l\in N(k,j+1)}L(l)\right]$$

9   where $b_0^{reg} = -\dfrac{61}{5720}$ and $b_1^{reg} = -\dfrac{14403}{5720}$ and L(l) represent Laplacian values generated by the

10   Laplacian operator for points, identified by indices N(k,j+1), that neighbor the at least one of said

11   points.

40. A method as defined in claim 37 in which the coarse level mesh generator step includes the step of determining, for at least one of said points in a triangular mesh representation, comprising an irregular point, that is, a point whose valence "K" is not equal to "six," and is not on a boundary, crease line or the like, for which the magnitude of the indicator value is below the selected threshold value, a position c^j(k) in the coarse level mesh representation in accordance with

$$c^J(k) = c^{J+1}(k) + \lambda\ L(k,j+1)$$

6   where $c^{J+1}(k)$ represents the position of the corresponding point in the finer level mesh representation,

7   L(k,j+1) represents the Laplacian value generated during the Laplacian generator step for the point

8   in the finer level mesh representation, and λ represents a parameter whose value is generated in

9   accordance with $\lambda = \dfrac{1}{L(k)}\left[b_0^{irreg}\ L(k) + \dfrac{1}{K}b_1^{irreg}\sum_{l\in N(k,j+1)}L(l)\right]$, where

$$b_0^{irreg} = \frac{2\left(5 - 8a(K)\right)\left(14647\,K - 391848\,a(K) + 391848\,a(k)^2\right)}{715\left(3 + 8\,a(k)\right)\left(256 + 41K - 512\,a(k) + 256\,a(k)^2\right)}$$

and

$$b_1^{irreg} = \frac{16\left(-5531K - 24521\,a(K) + 24521\,a(K)^2\right)}{715\left(256 + 41K - 512\,a(K) + 25\,a(K)^2\right)}$$

and where $\quad a(K) \quad = \quad \dfrac{5}{8} - \left(\dfrac{3 + 2\cos\left(\dfrac{2\pi}{K}\right)}{8}\right)^2 \quad .$

41. A method as defined in claim 37 in which the coarse level mesh generator step includes the step of determining, for at least one of said points, comprising a point on a boundary, crease line or the like in a quadrilateral mesh representation, for which the magnitude of the indicator value is not below the selected threshold value, a position $c^j(k)$ in the coarse level mesh representation in accordance with

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$$c^J(k) \;=\; c^{J+1}(k) + \lambda\, L\big(k, j+1\big)$$

6   where $c^{j+1}(k)$ represents the position of the corresponding point in the finer level mesh representation,

7    $L(k,j+1)$ represents the Laplacian value generated during the Laplacian generator step for the point

8   in the finer level mesh representation, and λ represents a parameter whose value is generated in

9   accordance with

$$\lambda \;=\; \frac{1}{L(k)}\left[b_0^{1D}\, L(k) + \frac{1}{2} b_1^{1D}\big(L(k-1) + L(k+1)\big)\right]$$

where $b_0^{1D} = -\dfrac{12}{35}$ and $b_1^{1D} = -\dfrac{23}{49}$, and L(k-1) and L(k+1) represent Laplacian values generated

during the Laplacian generator step for neighboring points in the finer level mesh representation.

42. A method as defined in claim 37 in which the coarse level mesh generator step includes the step

2   of determining, for at least one of said points in a quadrilateral mesh representation, which is not on

3   a boundary, crease line or the like, for which the magnitude of the indicator value is below the

4   selected threshold value, a position $c^j(k)$ in the coarse level mesh representation in accordance with

$$c^J(k) \;=\; c^{J+1}(k) + \lambda_1\, L_e\big(k, j+1\big) + \lambda_2\, L_f\big(k, j+1\big)$$

5   where $c^{j+1}(k)$ represents the position of the corresponding point in the finer level mesh representation,

6    $L_e(k,j+1)$ and $L_f(k,j+1)$ represent Laplacian values generated during the Laplacian generator step for

7   the point in the finer level mesh representation, and λ_1 and λ_2 represent parameters whose values are

8   generated in accordance with

$$\lambda_1 \;=\; \frac{1}{L_e(k,j+1)}\left[b_{10}^{cc}\, L_c\big(k,j+1\big) + \frac{1}{K}\, b_{11}^{cc} \sum_{l\in N(k,j+1)} L_e\big(l,j+1\big) \right]$$

9   and

$$\lambda_2 \;=\; \frac{1}{L_f(k,j+1)}\left[b_{20}^{cc}\, L_f\big(k,j+1\big) + \frac{1}{K}\, b_{21}^{cc} \sum_{l\in N_f(k,j+1)} L_f\big(l,j+1\big) \right]$$

10   where, if the at least one of said points is regular, that is, if its valence "K" is "four,"

$$b_{10}^{cc} \;=\; -\frac{9946871}{4862025}$$

$$b_{11}^{cc} \;=\; -\frac{1024}{405}$$

$$b_{20}^{cc} \;=\; \frac{1644032}{972405}$$

$$b_{21}^{cc} \;=\; -\frac{1338874}{972405}$$

11   and, if the at least one point is irregular, that is, its valence "K" is other than "four,"

$$b_{10}^{cc} = \frac{162307143936 - 92746939392\,K - 8924282387\,K^3}{4862025\left(12544 - 14336\,K + 4096\,K^2 + 901\,K^3\right)}$$

$$b_{11}^{cc} = \frac{1024\left(2793728 - 1596416\,K - 244001\,K^3\right)}{99225\left(12544 - 14336\,K + 4096\,K^2 + 901\,K^3\right)}$$

$$b_{20}^{cc} = \frac{512\left(-113305472 + 64745984K + 17391149\,K^3\right)}{4862025\left(12544 - 14336K + 4096\,K^2 + 901\,K^3\right)}$$

$$b_{21}^{cc} = \frac{4\left(8660934688 - 4949105536\,K - 1876158821\,K^3\right)}{4862025\left(12544 - 14336\,K + 4096\,K^2 + 901\,K^3\right)}$$

43. A computer program product for use in connection with a computer to provide a fine-to-coarse level mesh generating arrangement for generating a coarse level mesh representation representing a surface, from a finer level mesh representation, the computer program product comprising a computer-readable medium having encoded thereon:

A.   an indicator value generator module configured to enable the computer to, for respective ones of the points in the finer level surface representation, evaluate an indicator function to generate an indicator value, the indicator value indicating whether one a subdivision-inverse filter methodology or a least-squares optimization methodology is to be used to determine a position for a corresponding point in the coarse level mesh representation; and

B.   a coarse level mesh generator module configured to enable the computer to determine, for each of the points that are to be provided in the coarse level mesh representation, a position in the coarse level mesh representation in response to the position of the corresponding point in the finer level mesh representation, in accordance with the one of the subdivision-inverse filter methodology and least-squares optimization methodology as indicated by the indicator value.

1   44. A computer program product as defined in claim 43 further comprising a Laplacian generator

2   module configured to enable the computer to generate a Laplacian value for said respective ones of

3   the points in the finer level mesh representation.

1   45. A computer program product as defined in claim 44 in which the Laplacian generator module

2   is configured to enable the computer to generate the Laplacian value L(k,j+1), for at least one of said

3   points, said at least one of said points comprising a point on a boundary, crease line or the like in a

4   triangular mesh representation, in accordance with

$$L(k, j+1) \;=\; \frac{1}{2}\left[c^{J+1}(k-1) + c^{J+1}(k+1)\right] - c^{J+1}(k)$$

5   where $c^{j+1}(k)$ represents the position of the point for which the Laplacian is being generated in the

6   finer level mesh representation, and $c^{j+1}(k-1)$ and $c^{j+1}(k+1)$ represent the positions of neighboring

7   points in the finer level mesh representation.

1   46. A computer program product as defined in claim 44 in which the Laplacian generator module

2   is configured to enable the computer to generate the Laplacian value L(k,j+1), for at least one of said

3   points, said at least one of said points comprising a regular vertex, that is, for a vertex for which the

4   valence "K" is equal to "six," in a triangular mesh representation, in accordance with

$$L(k, j+1) \;=\; \frac{1}{6}\left(\sum_{l \in N(k,J+1)} c^{J+1}(l)\right) - c^{J+1}(k)$$

5   where $c^{j+1}(k)$ represents the position of the point for which the Laplacian is being generated in the

6   finer level mesh representation, and $c^{j+1}(l)$ represents the positions of neighboring points in the finer

7   level mesh representation.

1   47. A computer program product as defined in claim 44 in which the Laplacian generator module

2   is configured to enable the computer to generate the Laplacian value L(k,j+1), for at least one of said

3   points, said at least one of said points comprising a for a irregular vertex, that is, for a vertex for

4   which the valence "K" is not equal to "six," in a triangular mesh representation, in accordance with

$$L(k, j+1) \;=\; \rho \left[\frac{1}{K} \sum_{l \in N(k,J+1)} c^{J+1}(l) - c^{J+1}(k) \right]$$

5   where $c^{j+1}(k)$ represents the position of the point for which the Laplacian is being generated in the

6   finer level mesh representation, and $c^{j+1}(l)$ represents the positions of neighboring points in the finer

7   l e v e l   m e s h   r e p r e s e n t a t i o n , $\rho \;=\; -\dfrac{3 + 8\, a(K)}{3\left(-5 + 8\, a(K)\right)},$ a n d

8    $$a(K) \;=\; \frac{5}{8} - \left(\frac{3 + 2\cos\left(\dfrac{2\pi}{K}\right)}{8} \right)^2 .$$

1   48. A computer program product as defined in claim 44 in which the Laplacian generator module

2   is configured to enable the computer to generate the Laplacian value L(k,j+1), for at least one of said

3   points, said at least one of said points comprising a point on a boundary, crease line or the like in a

4   quadrilateral mesh representation, in accordance with

$$L(k, j+1) \;=\; \frac{1}{2}\left(c^{J+1}(k-1) + c^{J+1}(k+1)\right) - c^{J+1}(k) \qquad (101)$$

where $c^{J+1}(k)$ is the position of the vertex for which the Laplacian is being generated, and $c^{J+1}(k-1)$ and $c^{J+1}(k+1)$ are the positions of the neighboring points in the fine level mesh representation.

49. A computer program product as defined in claim 44 in which the Laplacian generator module is configured to enable the computer to generate Laplacian values $L_e(k,j+1)$ and $L_f(k,j+1)$, for at least one of said points, said at least one of said points comprising a point on a boundary, crease line or the like in a quadrilateral mesh representation, in accordance with

$$L_e(k, j+1) \;=\; \frac{1}{K}\left(\sum_{l \in N_e(k,J+1)} c^{J+1}(l)\right) - c^{J+1}(k)$$

5   and

$$L_f(k, j+1) \;=\; \frac{1}{K}\left(\sum_{l \in N_f(k,J+1)} c^{J+1}(l)\right) - c^{J+1}(k)$$

6   where $N_e(k,j+1)$ references a set of points comprising first order neighbors of the at least one of said

7   points in the finer level mesh representation, and $N_f(k,j+1)$ references a set of points comprising

8   second order neighbors of the at least one operating system said points in the finer level mesh

9   representation.

1   50. A computer program product as defined in claim 49 in which the coarse level mesh generator

2   module is configured to enable the computer to determine, for at least one of the points that are to

3   be provided in the coarse level mesh representation, the position in the coarse level mesh

4   representation as the position of the corresponding point in the finer level mesh representation if the

5   magnitude both Laplacian values $L_e(k,j+1)$ and $L_f(k,j+1)$ generated during processing under control

6   of the Laplacian generator module are below a predetermined threshold value.

1   51. A computer program product as defined in claim 44 in which the coarse level mesh generator

2   module is configured to enable the computer to determine, for at least one of the points that are to

3   be provided in the coarse level mesh representation, the position in the coarse level mesh

4   representation as the position of the corresponding point in the finer level mesh representation if the

5   magnitude of the Laplacian value generated during processing under control of the Laplacian

6   generator module is below a predetermined threshold value.

1   52. A computer program product as defined in claim 44 in which the coarse level mesh generator

2   module is configured to enable the computer to determine, for each of the points that are to be

3   provided in the coarse level mesh representation, a position in the coarse level mesh representation

4   in response to the position of the corresponding point in the finer level mesh representation, in

5   accordance with the subdivision-inverse filter methodology if the magnitude of the indicator value

6   is below a selected threshold value.

1   53. A computer program product as defined in claim 52 in which the coarse level mesh generator

2   module is configured to enable the computer to determine, for at least one of said points, comprising

3   a point on a boundary, crease line or the like in a triangular mesh representation, for which the

4   magnitude of the indicator value is below the selected threshold value, a position $c^j(k)$ in the coarse

5   level mesh representation in accordance with

$$c^J(k) \;=\; c^{J+1}(k) + \lambda\, L(k, j+1)$$

6   where $c^{j+1}(k)$ represents the position of the corresponding point in the finer level mesh representation,

7    $L(k,j+1)$ represents the Laplacian value generated during processing under control of the Laplacian

8   generator module for the point in the finer level mesh representation, and λ represents a parameter

9   whose value is $\lambda \;=\; -1$.

1   54. A computer program product as defined in claim 52 in which the coarse level mesh generator

2   module is configured to enable the computer to determine, for at least one of said points in a

3   triangular mesh representation, comprising a regular point, that is, a point whose valence "K" is

4   equal to "six," and is not on a boundary, crease line or the like, for which the magnitude of the

5   indicator value is below the selected threshold value, a position $c^j(k)$ in the coarse level mesh

6   representation in accordance with

$$c^J(k) \;=\; c^{J+1}(k) + \lambda\, L(k, j+1)$$

7   where $c^{j+1}(k)$ represents the position of the corresponding point in the finer level mesh representation,

8     $L(k,j+1)$ represents the Laplacian value generated during processing under control of the Laplacian

9   generator module for the point in the finer level mesh representation, and λ represents a parameter

10   whose value is $\lambda = -\dfrac{3}{2}$.

55. A computer program product as defined in claim 52 in which the coarse level mesh generator module is configured to enable the computer to determine, for at least one of said points in a triangular mesh representation, comprising an irregular point, that is, a point whose valence "K" is not equal to "six," and is not on a boundary, crease line or the like, for which the magnitude of the indicator value is below the selected threshold value, a position $c^j(k)$ in the coarse level mesh representation in accordance with

$$c^J(k) = c^{J+1}(k) + \lambda\, L(k, j+1)$$

7   where $c^{j+1}(k)$ represents the position of the corresponding point in the finer level mesh representation,

8     $L(k,j+1)$ represents the Laplacian value generated during processing under control of the Laplacian

9   generator module for the point in the finer level mesh representation, and λ represents a parameter

10   whose value is generated in accordance with

$$\lambda = \frac{8\,a(K)}{-5 + 8\,a(K)}$$

11

$$\text{where } a(K) \ = \ \frac{5}{8} - \left(\frac{3 + 2\cos\left(\frac{2\pi}{K}\right)}{8}\right)^2 .$$

12

56. A computer program product as defined in claim 52 in which the coarse level mesh generator module is configured to enable the computer to determine, for at least one of said points, comprising a point on a boundary, crease line or the like in a quadrilateral mesh representation, for which the magnitude of the indicator value is below the selected threshold value, a position $c^j(k)$ in the coarse level mesh representation in accordance with

$$c^J(k) \ = \ c^{j+1}(k) + \lambda\, L(k, j+1)$$

6   where $c^{j+1}(k)$ represents the position of the corresponding point in the finer level mesh representation,

7     $L(k,j+1)$ represents the Laplacian value generated during processing under control of the Laplacian

8   generator module for the point in the finer level mesh representation, and λ represents a parameter

9   whose value is $\lambda \ = \ -1$.

1   57. A computer program product as defined in claim 52 in which the coarse level mesh generator

2   module is configured to enable the computer to determine, for at least one of said points in a

3   quadrilateral mesh representation, which is not on a boundary, crease line or the like, for which the

4   magnitude of the indicator value is below the selected threshold value, a position $c^j(k)$ in the coarse

5   level mesh representation in accordance with

$$c^j(k) \;=\; c^{j+1}(k) + \lambda_1 \, L_e\big(k, j+1\big) + \lambda_2 \, L_f\big(k, j+1\big)$$

6   where $c^{j+1}(k)$ represents the position of the corresponding point in the finer level mesh representation,

7     $L_e(k,j+1)$ and $L_f(k,j+1)$ represent Laplacian values generated during processing under control of the

8   Laplacian generator module for the point in the finer level mesh representation, and λ_1 and λ_2

9   represent parameters whose values are generated in accordance with, if the valence "K" of the point

10   not equal to "three,"

$$\lambda_1 \;=\; -\frac{4}{K-3}$$

$$\lambda_2 \;=\; \frac{1}{K-3}$$

11   and, if the valence "K" for the vertex is equal to "three,"

$$\lambda_1 = -8, \quad \lambda_2 = 2$$

.

1 58. A computer program product as defined in claim 44 in which the coarse level mesh generator

2 module is configured to enable the computer to determine, for each of the points that are to be

3 provided in the coarse level mesh representation, a position in the coarse level mesh representation

4 in response to the position of the corresponding point in the finer level mesh representation, in

5 accordance with the least-squares optimization methodology if the magnitude of the indicator value

6 is above a selected threshold value.

1 59. A computer program product as defined in claim 58 in which the coarse level mesh generator

2 module is configured to enable the computer to determine, for at least one of said points, comprising

3 a point on a boundary, crease line or the like in a triangular mesh representation, for which the

4 magnitude of the indicator value is not below the selected threshold value, a position $c^j(k)$ in the

5 coarse level mesh representation in accordance with

$$c^J(k) \quad = \quad c^{J+1}(k) + \lambda \; L(k, j + 1)$$

6 where $c^{j+1}(k)$ represents the position of the corresponding point in the finer level mesh representation,

7 L(k,j+1) represents the Laplacian value generated during processing under control of the Laplacian

8 generator module for the point in the finer level mesh representation, and λ represents a parameter

9 whose value is generated in accordance with

$$\lambda \quad = \quad \frac{1}{L(k)} \left[b_0^{1D} \; L(k) + \frac{1}{2} b_1^{1D} \left(L(k - 1) + L(k + 1) \right) \right]$$

10 where $b_0^{1D} = -\dfrac{12}{35}$ and $b_1^{1D} = -\dfrac{23}{49}$, and L(k-1) and L(k+1) represent Laplacian values generated

11 during processing under control of the Laplacian generator module for neighboring points in the

12 finer level mesh representation.

1 60. A computer program product as defined in claim 58 in which the coarse level mesh generator

2 module is configured to enable the computer to determine, for at least one of said points in a

3 triangular mesh representation, comprising a regular point, that is, a point whose valence "K" is

4 equal to "six," and is not on a boundary, crease line or the like, for which the magnitude of the

5 indicator value is not below the selected threshold value, a position $c^J(k)$ in the coarse level mesh

6 representation in accordance with

$$c^J(k) = c^{J+1}(k) + \lambda\, L(k, j+1)$$

7 where $c^{J+1}(k)$ represents the position of the corresponding point in the finer level mesh representation,

8 L(k,j+1) represents the Laplacian value generated during processing under control of the Laplacian

9 generator module for the point in the finer level mesh representation, and λ represents a parameter

10 whose value is

$$\lambda = \frac{1}{L(k)}\left[b_0^{reg}\, L(k) + \frac{1}{6} b_1^{reg} \sum_{l \in N(k,J+1)} L(l) \right]$$

11 where $b_0^{reg} = -\dfrac{61}{5720}$ and $b_1^{reg} = -\dfrac{14403}{5720}$ and L(l) represent Laplacian values generated during

12 processing under control of the Laplacian operator for points, identified by indices N(k,j+1), that

13 neighbor the at least one of said points.

1 61. A computer program product as defined in claim 58 in which the coarse level mesh generator

2 module is configured to enable the computer to determine, for at least one of said points in a

3 triangular mesh representation, comprising an irregular point, that is, a point whose valence "K" is

4 not equal to "six," and is not on a boundary, crease line or the like, for which the magnitude of the

5 indicator value is below the selected threshold value, a position $c^j(k)$ in the coarse level mesh

6 representation in accordance with

$$c^J(k) = c^{J+1}(k) + \lambda\, L(k, j+1)$$

7 where $c^{J+1}(k)$ represents the position of the corresponding point in the finer level mesh representation,

8 L(k,j+1) represents the Laplacian value generated during processing under control of the Laplacian

9 generator module for the point in the finer level mesh representation, and λ represents a parameter

10 whose value is generated in accordance with $\lambda = \dfrac{1}{L(k)}\left[b_0^{irreg}\, L(k) + \dfrac{1}{K} b_1^{irreg} \sum_{l \in N(k,J+1)} L(l) \right]$, where

$$b_0^{irreg} = \frac{2\left(5 - 8a(K)\right)\left(14647\,K - 391848\,a(K) + 391848\,a(k)^2\right)}{715\left(3 + 8\,a(k)\right)\left(256 + 41K - 512\,a(k) + 256\,a(k)^2\right)}$$

11   and

$$b_1^{irreg} = \frac{16\left(-5531K - 24521\,a(K) + 24521\,a(K)^2\right)}{715\left(256 + 41K - 512\,a(K) + 25\,a(K)^2\right)}$$

12   and where $a(K) = \dfrac{5}{8} - \left(\dfrac{3 + 2\cos\left(\dfrac{2\pi}{K}\right)}{8}\right)^2 \quad.$

1   62. A computer program product as defined in claim 58 in which the coarse level mesh generator

2   module is configured to enable the computer to determine, for at least one of said points, comprising

3   a point on a boundary, crease line or the like in a quadrilateral mesh representation, for which the

4   magnitude of the indicator value is not below the selected threshold value, a position $c^j(k)$ in the

5   coarse level mesh representation in accordance with

$$c^J(k) = c^{J+1}(k) + \lambda\,L(k, j+1)$$

6 where $c^{j+1}(k)$ represents the position of the corresponding point in the finer level mesh representation,

7 $L(k,j+1)$ represents the Laplacian value generated during processing under control of the Laplacian

8 generator module for the point in the finer level mesh representation, and λ represents a parameter

9 whose value is generated in accordance with

$$\lambda \;=\; \frac{1}{L(k)}\left[b_0^{1D}\, L(k) + \frac{1}{2} b_1^{1D}\left(L(k-1) + L(k+1)\right)\right]$$

10 where $b_0^{1D} = -\dfrac{12}{35}$ and $b_1^{1D} = -\dfrac{23}{49}$, and $L(k-1)$ and $L(k+1)$ represent Laplacian values generated

11 during processing under control of the Laplacian generator module for neighboring points in the

12 finer level mesh representation.

63. A computer program product as defined in claim 58 in which the coarse level mesh generator

2 module is configured to enable the computer to determine, for at least one of said points in a

3 quadrilateral mesh representation, which is not on a boundary, crease line or the like, for which the

4 magnitude of the indicator value is below the selected threshold value, a position $c^j(k)$ in the coarse

5 level mesh representation in accordance with

$$c^J(k) \;=\; c^{J+1}(k) + \lambda_1\, L_e\big(k, j+1\big) + \lambda_2\, L_f\big(k, j+1\big)$$

6 where $c^{j+1}(k)$ represents the position of the corresponding point in the finer level mesh representation,

7 $L_e(k,j+1)$ and $L_f(k,j+1)$ represent Laplacian values generated during processing under control of the

8 Laplacian generator module for the point in the finer level mesh representation, and λ_1 and λ_2

9 represent parameters whose values are generated in accordance with

$$\lambda_1 = \frac{1}{L_e(k,j+1)}\left[b_{10}^{cc} L_c(k,j+1) + \frac{1}{K} b_{11}^{cc} \sum_{l \in N(k,j+1)} L_e(l,j+1)\right]$$

10   and

$$\lambda_2 = \frac{1}{L_f(k,j+1)}\left[b_{20}^{cc} L_f(k,j+1) + \frac{1}{K} b_{21}^{cc} \sum_{l \in N_f(k,j+1)} L_f(l,j+1)\right]$$

where, if the at least one of said points is regular, that is, if its valence "K" is "four,"

$$b_{10}^{cc} = -\frac{9946871}{4862025}$$

$$b_{11}^{cc} = -\frac{1024}{405}$$

$$b_{20}^{cc} = \frac{1644032}{972405}$$

$$b_{21}^{cc} = -\frac{1338874}{972405}$$

12   and, if the at least one point is irregular, that is, its valence "K" is other than "four,"

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$$b_{10}^{cc} = \frac{162307143936 - 92746939392\,K - 8924282387\,K^3}{4862025\left(12544 - 14336\,K + 4096\,K^2 + 901\,K^3\right)}$$

$$b_{11}^{cc} = \frac{1024\left(2793728 - 1596416\,K - 244001\,K^3\right)}{99225\left(12544 - 14336\,K + 4096\,K^2 + 901\,K^3\right)}$$

$$b_{20}^{cc} = \frac{512\left(-113305472 + 64745984K + 17391149\,K^3\right)}{4862025\left(12544 - 14336K + 4096\,K^2 + 901\,K^3\right)}$$

$$b_{21}^{cc} = \frac{4\left(8660934688 - 4949105536\,K - 1876158821\,K^3\right)}{4862025\left(12544 - 14336\,K + 4096\,K^2 + 901\,K^3\right)}$$